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# Analysis of TSP Optimization Problems using Genetic Algorithm

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# ABSTRACT

Initiation of this paper demarcates Genetic Algorithm, as it paradigm shift in soft computing to solve optimization problems. This paper perposed the application of GAs to TSP by examining combinations on different algorithms for the binary and unary operators used to generate better solutions and minimize the search space calls. Operational view of genetic Algorithm to solve TSP.

This paper describes the number of crossover operators and mutation operators that can be applied with path representation in order to solve TSP. The TSP is, given a collection of cities, the problem is to determine the shortest route which visits each city precisely once and then returns to its starting point.TSP is complex as it is a NP-complete problem. This literature proposes a heuristic approach for solving TSP with Genetic Algorithm as TSPGA. Genetic algorithm (GA's) has been used as search techniques on many NP (Non-Deterministic Polynomial Time) problems. Three binary and two unary operators were tested To find shortest path that travels through every city in a provided set of cities exactly once and travels back to the initial city. It is a faster solution but not necessarily an optimal solution.

Keywords Genetic Algorithms (GA); Mutation Operator; Crossover Operator TSPGA.

# **1.0 Introduction**

The concept of globalization has resulted in dissolution of boundary and the world shrinks to a global village. The happening in one part of the world affects the life of people living in the other part of the world i.e. the world has became highly cohesive and interconnected and life in insulation has no meaning.

The present 21<sup>st</sup> century in undergoing a major revolutionary change where technology has intervened in all works of life to make it social, economic, political or cultural.

Education is no expectation to be advisory affected by the intervened of technology and it has also seen many appropriate changes that has brought a totally new look to the concept of education in modern times.

With the technologically advanced word, the teacher should be aware of the new technologies and the way to integrated them in education so as to enhance learning in their students which is the major aim of education. Teachers of all levels of education should be able to incorporate new technologies and their impact lessons through latest trends that will affects at the cognitive domain of the learner to greater extent.

The relatively recent change from the term information technology to Information and Communication technology reflects the accelerated pattern in which modern technology has impacted teaching.

ICT covers not just computer but any technology involved in communication. In other word ICT is an umbrella term that includes any communication device like software, CD Rom, Internet, including still and video, cameras, e-contact, e-books and multimedia representations.

- 1. Definition of the objective function
- 2. Definition and implementation of the genetic representation.
- 3. Definition and implementation of the genetic operators. Once these three have been defined, the genetic algorithm should work fairly well.

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## 2.0 Problem Definition

Path representation have been many different representations used to solve the TSP problem using genetic algorithms (GA) as

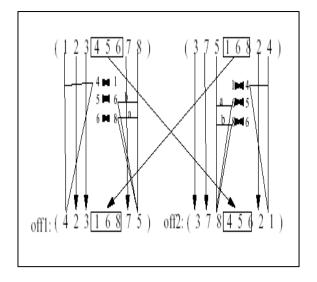
- Binary representation,
- Matrix representation,
- Adjacency representation,
- Ordinal representation
- Path representation

### **3.0 Operators**

There are number of crossover operators and mutation operators that can be applied with path representation in order to solve TSP. A portion of one parent's string is mapped onto a portion of the other parents string and the remaining information is exchanged.

### Example

Two parent tours (12345678) and (37516824)



First, it selects uniformly at random two cut points along the strings, which represent the parent's tours. The sub strings between the cut points are called the mapping sections. In the above example they define the mapping 4-1, 5-6, and 6-8. Now the mapping section of the first parent is copied into the second offspring and the mapping section of the second parent is copied into the first offspring.

### Iffspring1 (xxx168xx) and offspring2 (xxx456xx)

Then offspring 'i' ('i'=1, 2) is filled up by copying the elements of the I-th parents. In case a city is already present in the offspring it is replaced according to the mapping. For example the first element of offspring 1 would be a 1 like the first element of the first parent. However there is already a 1 present in offspring1. Hence, because of the mapping 1-4 we choose the first element of the offspring 1 to be a 4. The second, third and seventh elements of offspring1 can be taken from the first parent. However, the last element of the offspring 1 would be an 8, which is already present. Because of the mapping 6-6 and 6-5, it is chosen to be a 5.

Hence

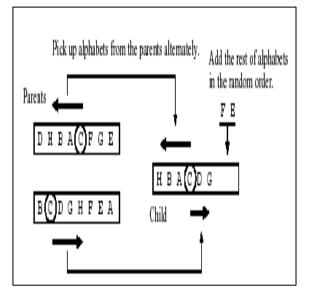
Offspring1 = (42316875) similarly Offspring2 = (37846521)

3.1 Greedy Sub tour crossover

Example

Consider a tour g=(DHBACFGE).

Fig 2: Greedy Subtour Crossover



Suppose that chromosomes of parents are

ga = (DHBACFGE) and gb = (BCDGHFEA).

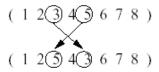
First, choose one town at random. In this example, town C is chosen. Then, x = 4 and y = 1 because a4 = C and b1 = C respectively. Now the child g is (C). Next, pick up towns from the parents alternately. Begin with a3 (town A) because x 4 - 1 =

3, and next is b2 (town D) because y 1+1 = 2. The child becomes g = (A;C;D). In the same way, add a2 (town B), b3 (town G), a1 (town H), and the child becomes g = (HBACDG). Now the next town is b4 = H and town H has already appeared in the child (remember the salesperson may not visit the same town twice), so we can't add any more towns from parent gb. Therefore we add towns from parent ga. The next town is a0 = D, but D is already used. Thus we can't add towns from parent ga, either. Then, we add the rest of the towns, i.e., E and F, to the child in the random order. Finally the child is g = (HBACDGFE).

### 3.2 Greedy exchange mutation

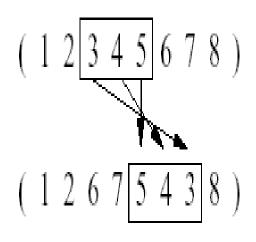
In this method two cities are selected randomly and exchanged.

### Fig 2. Exchange Mutation



#### 3.3 Inversion random displacement

In this method a sub tour is selected in random and it is removed from the tour and inserted it in a randomly selected position. However the sub tour is inserted in reverse order



The objective of TSP is to minimize the distance or path of the shortest length and the minimum cost on an undirected graph that represents cities or node to be visited. The successor of the last

node in the permutation is the first one. The Euclidean distance d, between any two cities with coordinate (x1, y1) and (x2, y2) is calculated by

$$d = \sqrt{(|X_1 - X_2|)2 + (|Y_1 - Y_2|)2}$$
(1)

## 4.0 Tsp Using GA

The work in this paper aims to develop a computer software system for solving the TSP based on Genetic Algorithm (TSPGA).

The number of cities involved in the search is entered and named as the letters  $\{a, b, c...\}$ , and then Euclidean distances between the cities are calculated or entered. An initial solution is generated as a sequence of letters. Then a fitness function is used and two solutions are selected leading to the emergence of a new born solution which replaces one of the parent solutions.

## 4.1 GA components

The successive generations are derived by applying the selection, crossover and mutation operators to the previous tour population.

### 4.2 The fitness function

A fitness function evaluation is incorporated to assigns a value to each organism, noted as fi. This fi value is a figure of merit which is calculated by using any domain knowledge that applies. The method employed here was to calculate the total Euclidean distance Di for each organism first, then compute *fi* by using the following equation

$$f_i = D_{max} - D_i$$

Where *Dmax* is the longest Euclidean distance over organisms in the population.

### 4.3 Selection operations

The selection operator chooses two members of the Mutation present generation to participate in the next operations of crossover and mutation

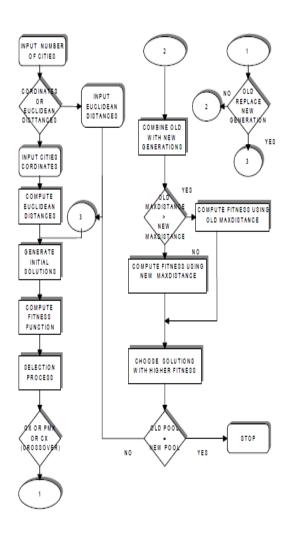
### 4.4.1 Specialized crossover operator

Two points crossover operator would have to be modified to work with such problems. Exchanging parts of two solutions will usually produce an invalid solution. Below an example that shows two parents of length 9. Select two random points in parents; say 3 and 6, then the alleles between those points are swapped to generate two children solutions. Both of the resulting children solutions are invalid [18].

Sr. No.	Orgnasim	Di	$\mathbf{f}_{i}$	Pi	Si
1	BEFCAD	122	0	0.01	1
2	FEBACD	101	21	0.10	2
3	CDAFBE	80	42	0.19	2
4	DAFCBE	50	72	0.31	2
5	BDAEFC	30	92	0.40	3

**Table 1: An Example for Path Fitness Function** 

# Fig 3: The Flow Diagram for TSP Using GA Software System



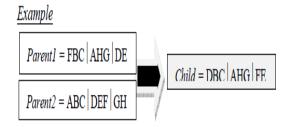
Three types of special crossover operators reported for permutation problems are selected to be examined and used in the proposed TSPGA system.

They are

Order crossover (OX), Partially matched crossover (PMX), and Cycle crossover (CX), as described briefly below.

## A. Order Crossover (Ox)

To apply OX, two random cross points are selected. Alleles from parent1 that fall between the two cross points are copied into the same positions of the offspring. The remaining allele order is determined by parent2. Non-duplicative alleles are copied from parent2 to the offspring beginning at the position following the second cross point. Both the parent2 and the offspring are traversed circularly from that point. A copy of the parent's next nonduplicative allele is placed in the next available child position [17]. An Example of OX is given below with two random cross points; 3 and 6, the alleles in the crossing sites from parent1 (GHB) are copied into the same positions of the child. The alleles after second cross point in parent2 (BA), B is skipped since it already exists in child, therefore only A is copied to child at position 7. Traverse parent2 circularly, the alleles (HDE), skip H to D which is copied to child at position 8. Traversed Child circularly, the alleles from parent2 (EF) are copied to child at positions 1 and 2. Finally, skip G to C and copy it to child at position 3.

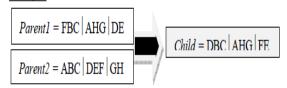


### **B.** Partially Matched Crossover

PMX proceeds just as OX. Alleles from parent1 that fall between two randomly selected crossing sites are copied into the same positions of the offspring first, alleles in parent2 not within crossing sites are copied to the corresponding positions within the offspring. Next each allele of parent2 within the crossing sites is placed in the offspring at the position occupied in parent2 by the allele from parent1 that displaced it [17], see the example below.

The random crossing points are 3 and 6, the alleles in the crossing site of parent1 (AHG) displace in the child (DEF), and then the alleles (BC) in parent2 which are not in crossing site are copied into the same positions of the child. D goes to position 1 which is the position with respect to parent2, displacing allele A. Finally E and F are placed in the positions of H and G, respectively.

Example

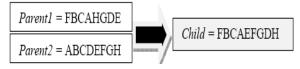


# **C. Cycle Crossover**

CX performs recombination under the constraint that each allele value comes from one parent or the other [19]. CX does not use crossing sites, but a cycle is defined in a manner similar to an algebraic permutation group [17], see the example below, Comparing the strings of parent1 with parent2, F displaces A, A displaces D, D displaces G,

and G displaces F. This forms the cycle FADG. The remaining alleles are filled from parent2 in the corresponding positions, BC, E, and H.

Example



## 4.4.2 Specialized mutation operator (SMX)

The mutation operator is a permutation problem arbitrarily changing single allele value that does not preserve allele uniqueness. The method frequently used for permutation problems is to interchange two randomly selected positions, thus preserving allele uniqueness [17]. The example below uses one of the previous child solutions. Let the crossing points be 2 and 6 selected randomly. The alleles B and G are swapped positions in the mutated child Solution.

# <u>Example:</u>



The system is designed to run in one of two options; default and customized as requested by the user. This is clearly shown in the flow diagram of Fig. 4.1

### A. Default System

The user enters the required data to produce solutions only, but he/she has neither influence nor choice to control the process. The selection of the crossover, mutation operations and mating pool strategies are chosen based on the experimental results, rather than user choice.

It is executed according to the following steps.

- 1- The system prompts to enter number of cities.
- 2- The system prompts to enter coordinates of cities, then it computes Euclidean distances between cities or they may be entered directly depends on user desire.
- 3- After distance matrix becomes available, the system generates randomly initial solutions and Computes longest Euclidean distance.
- 4- Finally the GA system continues processing till a solution is reached.

### **B.** Customized System

This option operates the system according to user choices. The system prompts to enter the required data as in default option, then prepares distance matrix.

The user has the selection of the followings

- 1- The version of crossover operator, i.e. OX, PMX, CX.
- 2- The strategy of maintaining the mating pool can be one of the following

Strategy1 the new generation replaces old generation.

Strategy2 the combination of old and new generations.

Choosing *strategy1* of the above have given noisy results and took long implementation time. Therefore, *strategy2* was adopted, which determines the longest (maximum) .The resulted solutions were sorted in descending order according to fitness value then the solution with higher fitness was chosen.

### 5.0 Results

GA as the name implies, this algorithm gets its idea from genetics.

### Algorithm 1

Step 0. Obtain the maximum number of individuals in the population P and the maximum number of generations G from the user, generate P solutions for the first generation's population randomly, and represent each solution as a string. Set generation counter Ngen=1.

Step 1. Determine the fitness of each solution in the current generation's population and record the string that has the best fitness.

Step 2. Generate solutions for the next generation's population as follows

1. Retain 0.1P of the solutions with the best fitness in the previous population.

2. Generate 0.89P solutions via mating, and

3. Select 0.01P solutions from the previous population randomly and mutate them.

Step 3. Update Ngen=Ngen+1. If Ngen  $\leq$  G, go to Step 1. Otherwise stop.

In our project, we used the two-point crossover method, given two parent chromosomes  $\{x1,x2,...,xn\}$  and  $\{y1,y2,...,yn\}$ , two integers r and s are randomly selected, such that  $1 \text{ \pounds r \pounds s \pounds n}$ . And the genes in positions r to s of one parent are swapped with those of the other to get two off springs as follows.

 ${x1, x2,..., xr-1, yr, yr+1,..., ys, xs+1, xs+2,..., xn}$ 

Either both or the better of the two offspring is then included in the new population.

This mutation procedure is repeated until the required number of offspring is generated. To avoid generating infeasible solutions, we also used the partially matched crossover method. Set t=r, and

swaps genes xt and yt if xt  $\neq$  yt in the first parent x={x1, x2... xr-1, xr, xr+1,..., xs, xs+1, xs+2,..., xn}. This swapping is done for t=r through s, one by one, and then we have a feasible offspring. The same is done for y={y1, y2,..., yr-1, yr, yr+1,..., ys, ys+1, ys+2,..., yn}. Because the partially matched crossover method always swaps genes within a parent, feasible offspring are obtained. Therefore, our model uses mutation to generate a population by swapping any two randomly selected genes.

### Algorithm 2

Step 1. Find the point jc which is closed to city i.

Step 2. Point jc is moved with its neighbors towards city i to form a ring. The moved distance is measured by function f(G,n).G is the gain factor and n is the distance measured along the loop between nodes j and jc.

n=inf (j- jc (mod N), jc -j(mod N))

Point j is moved from current position to a new one.

The function f is defined to be

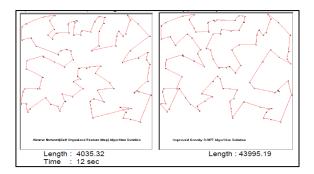
f(G,n)=sqrt(1/2)\*exp(-n2/G2)

This means

- When (G, n), all points move towards city I with the equal strength sqrt(1/2).

- When (G, n) only point jc travels towards city i.

Reducing the gain in the end of a complete survey is done by  $G \leftarrow (1-\alpha)G$ . The parameter  $\alpha$  is required to be adjusted .The parameter  $\alpha$  id related to the number of cities which are required to be monitored. The gain decreases from a high initial Gi which makes sure that large moves for all points in every iteration to a sufficiently small Gf for which the network is sustained. The newly made point is inserted as a neighbor to winner into the ring, and its coordinated are same in the plane.



## **6.0** Conclusions and Remarks

The TSPGA system was developed to assist the user to obtain optimal tour to visit n cities. It has proposed the use of advanced operators of Genetic Algorithms in order to enhance the rate of divergence, and achieved tours with reasonable time. It has used an interactive user interface enabling users to handle most system features. The developed selection algorithm used helps to select a suitable strategy for selecting a pair of parents for crossover operation. Besides, newly developed fitness function is

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